



# Modeling Rare Baseball Events – Are They Memoryless?

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**Key Words:** Anderson-Darling Goodness-of-Fit Test; Exponential Distribution; Hitting for the Cycle; Memoryless Property; No-Hit Games; Poisson Process; Triple Plays.

## Abstract

Three sets of rare baseball events – pitching a no-hit game, hitting for the cycle, and turning a triple play – offer excellent examples of events whose occurrence may be modeled as Poisson processes. That is, the time of occurrence of one of these events doesn't affect when we see the next occurrence of such. We modeled occurrences of these three events in Major League Baseball for data from 1901 through 2004 including a refinement for six commonly accepted baseball eras within this time period. Model assessment was primarily done using goodness of fit analyses on inter-arrival data.

## 1. Introduction

On June 29<sup>th</sup>, 1990, both Fernando Valenzuela of the Los Angeles Dodgers and Dave Stewart of the Oakland Athletics pitched no-hit games, the first time two pitchers from different leagues accomplished the rare feat of holding their opponents hitless on the same day. Even more amazing, in 1938, Johnny Vander Meer of the Cincinnati Reds pitched two no-hitters in successive starts (on June 10<sup>th</sup> and June 14<sup>th</sup>). Babe Herman, an outfielder with the Brooklyn Robins, is the only player in Major League Baseball history (since 1901) to hit for the cycle twice in the same season (1931). On July 17<sup>th</sup>, 1990, the Minnesota Twins turned two triple plays against the Boston Red Sox in the same game. Some events in baseball are more rare than others. Three of the more rare feats – pitching a no-hit game, hitting for the cycle, and turning a triple play – appear to be reasonably modeled as Poisson processes.

From 1901 through the end of the 2004 season, there were 206 official no-hit games pitched in the American and National Leagues. According to the [The Book of Baseball Records](#), there have been 13 “Near No-Hitters” in the Major Leagues from 1901 - 2004 (instances where the no-hitter had been broken up in extra innings), as well as 25 occurrences of a pitcher not allowing a hit in an official game that was less than nine innings. Because these events do not meet the criteria set forth by Major League Baseball (MLB) as being a “No-Hit Game,” we did not include them in the data. A no-hit game (commonly known in baseball as a “no-hitter”) refers to a game in which one of the teams has prevented the other team from getting an official hit during the entire length of the game, which must be at least 9 innings by the current Major League Baseball definition. During this time span there were 225 batters who hit for the cycle – batters who had a single, a double, a triple, and a home run in the same game. In addition, there were 511 times from 1901 – 2004 in which a team turned a triple play

in a game, which means that a team recorded three outs in an inning during a single at-bat. We only consider, by the way, regular season games in this article.

Obvious questions arise. First, how often do no-hitters, hitting for the cycle, and triple plays occur in a regular season? Also, can we model the number of each that we might expect to see in a season? Finally, do the chances of these events occurring change during different eras in baseball history?

## 2. Modeling Rare Events as Poisson Processes

These three rare incidents offer excellent examples of data that might be modeled by Poisson processes. The Poisson distribution is often used to characterize the occurrence of events of a particular type over time, area, or space. By definition, a random variable  $X$  is said to have a Poisson distribution if its probability mass function is

$$p(x; \lambda) = \frac{e^{-\lambda} \lambda^x}{x!},$$

for non-negative integers of  $x$  and some positive  $\lambda$ . For us the parameter  $\lambda$  will be a rate per unit time. Additionally, if  $X$  has a Poisson distribution with parameter  $\lambda$ , then both the expected value of  $X$  and the variance of  $X$  are equal to  $\lambda$ . If the annual number of no-hitters, cycles, and triple plays indeed follow Poisson processes, exponential distributions will model the distributions of times between consecutive occurrences. A random variable  $T$  is said to have an exponential distribution if its probability density function is

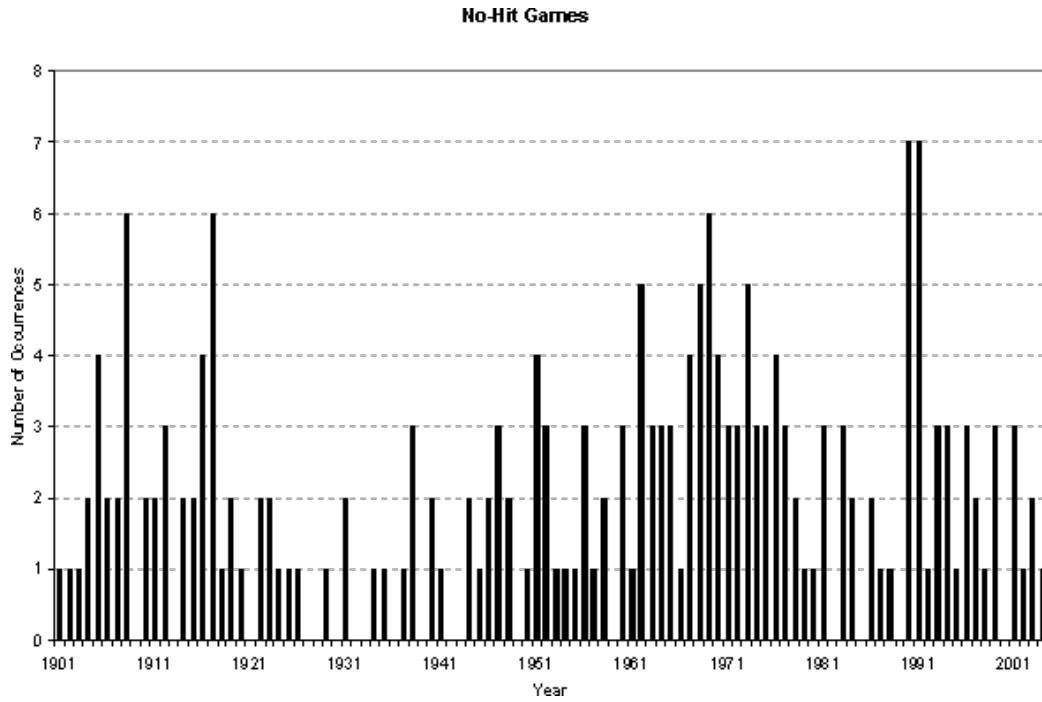
$$f(t; \lambda) = \begin{cases} \lambda e^{-\lambda t} & t \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

where  $\lambda > 0$ . Additionally, if  $T$  has an exponential distribution with parameter  $\lambda$ , then the expected value of  $T$  equals  $1/\lambda$  and the variance of  $T$  is equal to  $1/\lambda^2$ . Note, then, that the mean and standard deviation are equal.

An important distinction of the exponential distribution is its “memoryless” property. It is well known that the only continuous distribution that models a memoryless process is the exponential distribution. The memoryless property implies that the time of the last occurrence of an event does not affect the time to the next occurrence of that event. Intuitively, we believe this to be at least approximately true of our three baseball events.

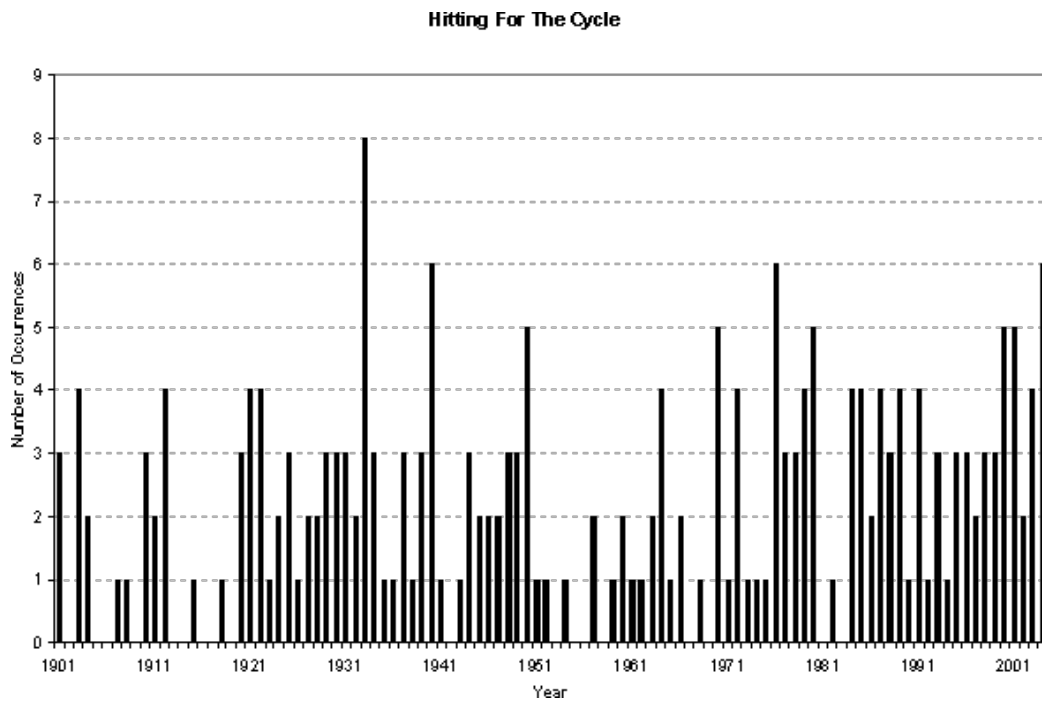
As mentioned earlier, from 1901 to 2004, there have been 206 no-hitters, 225 cycles, and 511 triple plays. These data can be readily found at a number of websites (see References). The most no-hitters pitched in a single season during this time period is eight, and the fewest is zero. There has been one season in which eight batters have hit for the cycle, and the fewest number of occurrences in a season is zero. There have been three seasons in which eleven triple plays have occurred, but only two seasons in which no triple play occurred.

[Figure 1](#), [Figure 2](#), and [Figure 3](#) show the total number of occurrences for no-hitters, cycles, and triple plays per year, respectively, for 1901 – 2004. All three events have a high number of years when only one, two, or three events occurred. Instances where more than three of each event occurred in a particular season were infrequent, especially in the no-hitter and cycles data sets (see [Table 1](#)). The mean number of no-hitters per year is  $\lambda = 1.98$ , or just about two no-hitters per season. The mean number of cycles over this period is  $\lambda = 2.16$ , and the mean for the number of triple plays over this period is  $\lambda = 4.91$ . Even though this last number is higher than for no-hitters or cycles, we will still consider triple plays to be rare events. To further indicate the rarity of these events, we note that from 1901 to 2004 there were 159,650 official games played. Consequently, roughly 0.13% of games were no-hitters, roughly 0.14% of games had a batter hit for the cycle, and roughly 0.32% of games had a triple play.



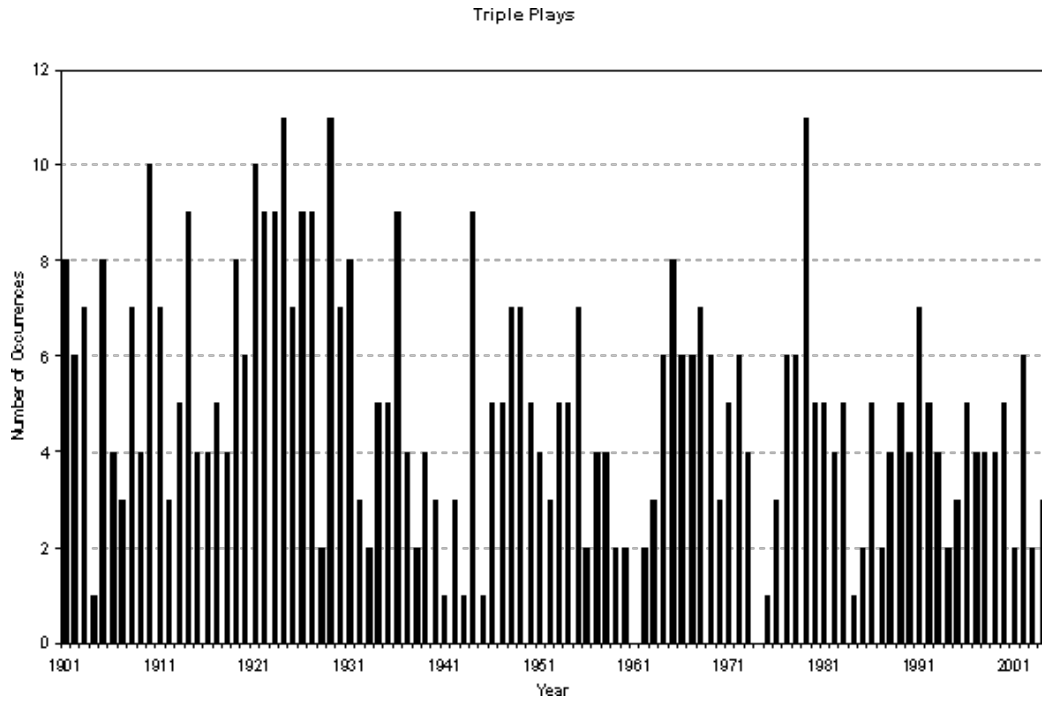
[Figure 1](#)

Figure 1. Number of No-Hit Games by Year (1901 – 2004).



[Figure 2](#)

Figure 2. Number of Cycles by Year (1901 – 2004).



[Figure 3](#)

Figure 3. Number of Triple Plays by Year (1901 – 2004).

Table 1. Actual (versus Estimated) Counts of Rare Events Per Season (1901-2004)

Count	No Hitters	Hit for Cycle	Triple Plays
0	18 (14.3)	18 (12.0)	2 (0.8)
1	30 (28.4)	27 (25.9)	6 (3.8)
2	21 (28.1)	16 (28.0)	12 (9.2)
3	21 (18.6)	21 (20.2)	12 (15.1)
4	6 (9.2)	13 (10.9)	17 (18.6)
5	3 (3.6)	5 (4.7)	18 (18.2)
6	3 (1.2)	3 (1.7)	9 (14.9)
7	2 (0.3)	0 (0.5)	11 (10.5)
8	0 (0.1)	1 (0.1)	5 (6.4)
9	0 (0.0)	0 (0.0)	7 (3.5)
10	0 (0.0)	0 (0.0)	2 (1.7)
11	0 (0.0)	0 (0.0)	3 (0.8)
12	0 (0.0)	0 (0.0)	0 (0.3)
Total	206	225	511
$\lambda = \bar{x}$	<b>1.98</b>	<b>2.16</b>	<b>4.91</b>
$s^2$	<b>2.64</b>	<b>2.90</b>	<b>6.66</b>

Using the probability mass function for the corresponding Poisson distribution, we can estimate the probability that there will be  $x$  rare events in a season (see [Table 2](#)). For example, the estimated probability that exactly six batters will hit for the cycle in a single season is

$$p(6; 2.16) = \frac{e^{-2.16} (2.16)^6}{6!} \approx 1.64 \%$$

That is, there is an estimated 1.64% chance that exactly six batters will hit for the cycle in a season. Further estimated chances are listed in [Table 2](#). Using [Table 2](#) we see, for example, that there is a 97.68% chance that fewer than six batters will hit for the cycle in a single season (interestingly, in the 2004 Major League season, six batters did hit for the cycle). Also, multiplying these estimated chances by 104 – the number of seasons from 1901 through 2004 – we get the estimated counts displayed in [Table 1](#).

Table 2. Estimated Probabilities of Rare Events Occurring Per Year Using the Poisson Distribution Model and Estimated Mean

#	No Hitters	Hit for Cycle	Triple Plays
0	13.80%	11.49%	0.73%
1	27.33%	24.86%	3.61%
2	27.06%	26.90%	8.87%
3	17.87%	19.40%	14.53%
4	8.85%	10.49%	17.84%
5	3.51%	4.54%	17.53%
6	1.16%	1.64%	14.36%
7	0.33%	0.51%	10.08%
8	0.08%	0.14%	6.19%
9	0.02%	0.03%	3.38%
10	0.00%	0.01%	1.66%
11	0.00%	0.00%	0.74%
12	0.00%	0.00%	0.30%
13	0.00%	0.00%	0.11%
14	0.00%	0.00%	0.04%
15	0.00%	0.00%	0.01%

Estimating the number of seasonal occurrences of any one of our rare phenomena by a single Poisson is at best questionable as, among other things, the number of games played during a season has varied over time. Everything else being equal, seasons with a greater number of games will tend to produce greater numbers of our rare events. As a refinement to the modeling process just presented, in Section 4 we look at separate models for each of several smaller, more homogeneous eras over the 1901 – 2004 time period.

### 3. Calculating Inter-Arrival Times

For simplicity of presentation, we delay modeling over individual eras for now to give an alternative analysis to that presented above. Instead of checking whether annual counts follow Poisson distributions, we may examine inter-arrival times (the number of games between each type of event) to see if they follow exponential distributions. On May 5<sup>th</sup>, 1917, Ernie Koob of the St. Louis Browns no-hit the Chicago White Sox by a score of 1 – 0. It was the 132<sup>nd</sup> game of the season. We used an algorithm to calculate the game number. We went to [www.retrosheet.org](http://www.retrosheet.org), an Internet site which contains the standings at the end of each day of the season. We would count the total number of games played in the Major

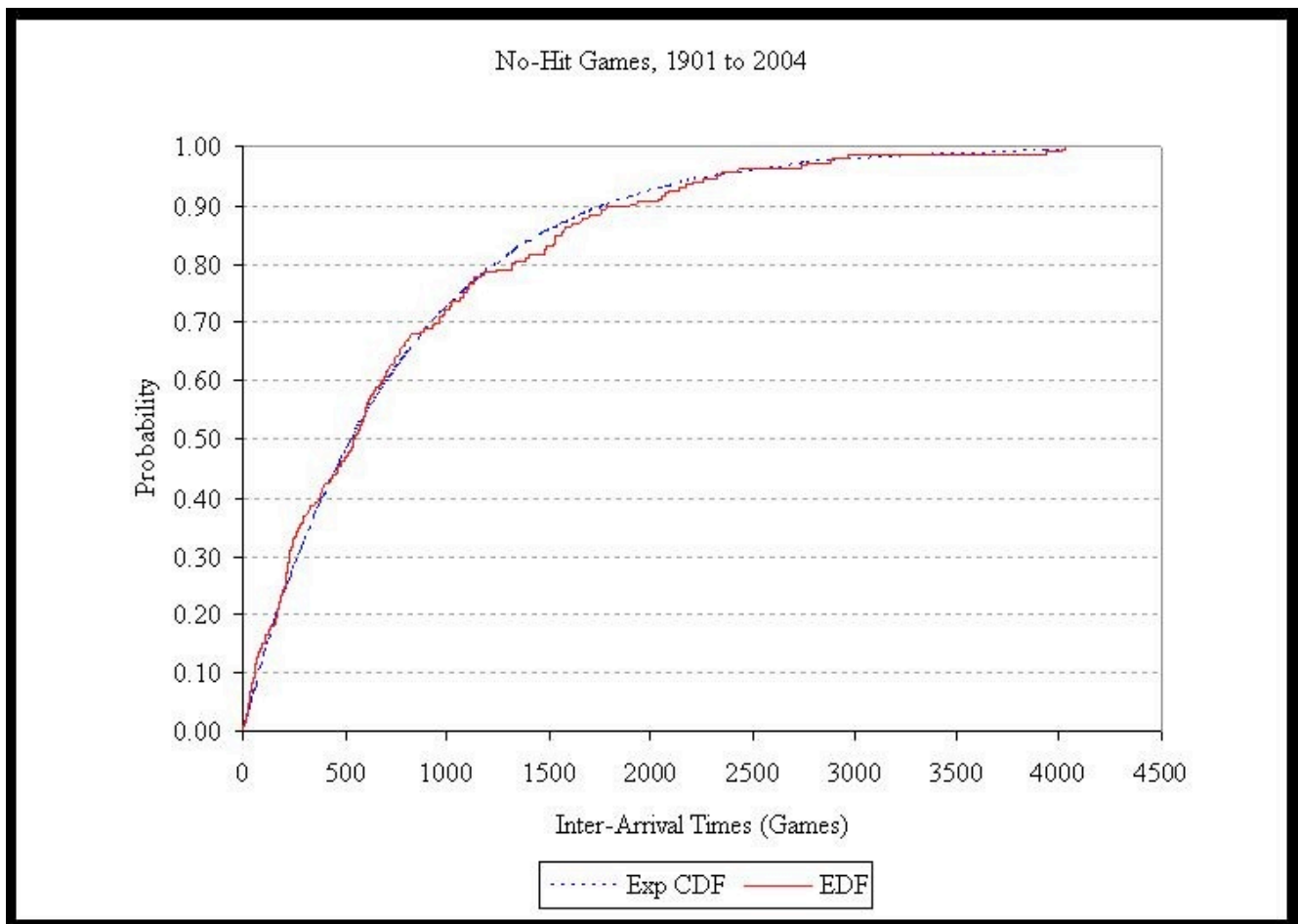
Leagues at the end of the day before an event. For example, Lou Gehrig hit for the cycle on June 25<sup>th</sup>, 1934. The standings at close of play on June 24<sup>th</sup> (the previous day) listed 982 total games. Because it takes two teams for a game, we divided 982 by 2 to obtain 492. We then added 1 to obtain 492. It is virtually impossible to determine the order of the games on a certain day at the beginning of the 20<sup>th</sup> century, so we assumed that each game with a rare event was the first of its day. Therefore, we count Lou Gehrig's cycle as occurring during the 492<sup>nd</sup> game of the season. We were consistent with this algorithm throughout the no-hitter, hitting for the cycle, and triple play data. Bobby Veach (Detroit Tigers, AL) and George Burns (New York Giants, NL) both hit for the cycle on the same day, September 17<sup>th</sup>, 1920, but in different games; we counted the two events as one game apart. The next no-hitter occurred on May 6<sup>th</sup>, when Koob's teammate Bob Groom also pitched a no-hitter against those same White Sox by a score of 3 – 0. It was the 135<sup>th</sup> game of the season. The inter-arrival time between these two no-hitters was three games. On June 23<sup>rd</sup>, 1917, Babe Ruth and Ernie Shore of the Boston Red Sox combined to pitch the next no-hitter (Ruth only faced one batter before being ejected for arguing balls and strikes) against the Washington Senators, by a score of 4 – 0. This was the 444<sup>th</sup> game of the 1917 season, so the inter-arrival time between Groom's no-hitter and the Ruth/Shore combined no-hitter was 309 games.

We calculated the inter-arrival times between successive no-hitters for every season from 1901 through 2004. Using box scores found online at [www.retrosheet.org](http://www.retrosheet.org), we verified that each game took place on the date given, then went to the previous day, counted all the wins and losses for all teams, and divided by two. The average inter-arrival time for a no-hitter is 772 games. Similarly, the average inter-arrival times for a cycle and triple play are 720 and 316 games, respectively.

At this point we discuss goodness-of-fit tests for the exponentiality of the data. In [Figure 4](#), we present a comparison of the empirical distribution function (EDF) with the fitted exponential cumulative distribution function (CDF) for no-hit games, using the estimated lambda. Similar EDF versus fitted CDF graphs for cycles and triple plays may, of course, be produced.

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[Figure 4](#)

Figure 4: EDF vs. Exponential CDF for No-Hit Games.

Graphically, no-hitter inter-arrival times seem to be well modeled by an exponential. We now look at formal statistical tests of an exponential model. We first consider Pearson's chi-square statistic. It is easy to understand, but as we will indicate, it is problematic for testing exponentiality. To illustrate the use of the chi-square statistic, we consider the no-hitter data. A cell count of those inter-arrival times, as well as what we would expect to see for each cell, is shown in [Table 3](#) below. Each line in the Table shows the interval for inter-arrival times in which 20 events occurred. For example, 20 no-hitters occurred with inter-arrival times ( $x$ ) of  $0 \leq x < 56$ . Similar tables could be constructed for cycles and triple plays.

Table 3. The Construction of the Chi-square Test Statistic for No-Hitters

IAT		Observed (obs)	Expected (exp)	(obs - exp) <sup>2</sup> /exp
≥	<			
0	56	20	14.4085	2.1699
56	162	20	24.5716	0.8505
162	221	20	12.2843	4.8462
221	328	20	20.0194	0.0000
328	530	20	31.0046	3.9059
530	638	20	13.5348	3.0882
638	820	20	18.9327	0.0602
820	1132	20	23.6778	0.5713
1132	1654	20	23.3695	0.4858
1654	2762	20	18.4333	0.1332
2762	4029	6	4.6461	0.3945

The sum of the last column in [Table 3](#) is about 16.5. The corresponding p-value, on 10 degrees of freedom, is about 0.09 indicating the exponential null hypothesis for no-hitters cannot be rejected at the 0.05 significance level. The chi-square test is based on binned data. Selection of the bin size for data sets is sometimes more of an art than a science. Some choose to select bins of equal width on the horizontal axis. We have chosen to create equi-probable bin sizes instead, as this bin-size method has been shown to be unbiased and more accurate for approximating the null hypothesis ([D'Agostino and Stephens, 1986, pg. 69](#)). The basic idea behind the chi-square test is that the observed number of points in each bin should be similar to the expected counts. For goodness-of-fit in general, while the chi-square statistic is easy to understand and implement, it is problematic and suffers low statistical power. It reduces continuous data into discrete cells; thus, we lose the resolution of each inter-arrival time. It is well established that such loss of fidelity makes the chi-square statistic lack power. That is, compared to more powerful tests, this test will accept a false null hypothesis more often.

Consequently, as noted by D'Agostino and Stephens (1986), with continuous data it is much more appropriate to use EDF-based statistics that measure the squared distance between the EDF and the exponential model, thus relying on the actual value of each observation. We used the Anderson-Darling  $A^2$  statistic for testing the fit of exponential distributions (as outlined on pages 134 – 135 of [D'Agostino and Stephens, 1986](#), a 'case 2, rate parameter unknown' test), and calculated adjusted test statistics of 0.81 for no-hitters (a p-value between 0.200 and 0.250), 1.03 for cycles (a p-value between 0.100 and 0.150), and a test statistic of 2.73 (a p-value less than 0.0025) for triple plays. For triple plays, there seems to be a significant departure from exponentiality. This will be further examined in the next section, where we will use the  $A^2$  statistic to examine exponentiality of our three rare events over eras within the 1901-2004 time frame.

## 4. Adjusting For Different Eras

Should we make an adjustment for the era in which players play? Baseball has, of course, changed over the last century. The total number of games played in a single season has changed, for example, whenever the leagues have expanded with more teams. (In the modern baseball season, there are 2430 games as each of 30 teams play 162 games. Back in 1917, by

way of contrast, there were only 16 teams who played between 154 and 158 games each, for a total of 1247 games.) Changes in the style of play and players also impact the number of rare events. There have been periods when pitching was dominant and other periods when hitting was dominant. Most baseball historians agree that there have been periods of change, and although everyone might not agree on the exact dates of different periods, those periods (subsets of the data) can be classified by the eras listed in [Table 4](#) (see [References](#) for source). Also listed are the number of rare occurrences for each era, by type.

Table 4: Historical Eras of Major League Baseball With Occurrences

<b>Era</b>	<b>Years</b>	<b>No-Hitters</b>	<b>Cycles</b>	<b>Triple Plays</b>
Dead Ball	1901 to 1919	43	22	107
Lively Ball	1920 to 1941	20	60	136
Integration	1942 to 1960	30	29	81
Expansion	1961 to 1976	56	31	66
Free Agency	1977 to 1993	37	46	81
Long Ball	1994 to 2004	20	37	40

Each rare event was thus divided into these six eras and the count, mean inter-arrival times (denoted as Mean IA below), and lambda values were estimated. This information is shown in [Table 5](#).

Table 5: Mean Inter-Arrival Times and Lambda Values Per Era

		<b>No-Hitter</b>	<b>No-Hitter</b>	<b>Cycles</b>	<b>Cycles</b>	<b>Triple Play</b>	<b>Triple Play</b>
<b>Era</b>	<b>Seasons</b>	<b>Mean IA</b>	$\lambda$	<b>Mean IA</b>	$\lambda$	<b>Mean IA</b>	$\lambda$
Dead Ball	19	536	2.26	959	1.16	213	5.63
Lively Ball	22	1344	0.91	449	2.73	199	6.18
Integration	19	788	1.58	798	1.53	285	4.26
Expansion	16	514	3.50	899	1.94	415	4.13
Free Agency	17	889	2.18	747	2.71	444	4.76
Long Ball	11	1164	1.82	665	3.36	613	3.64

There are clear differences between the eras. For example, during the Dead Ball Era, the mean inter-arrival time of no-hitters was low, while the mean inter-arrival time of cycles per year was high. These two trends were reversed during the Lively Ball Era. The mean inter-arrival time of triple plays did not change significantly during these two eras. The Expansion Era saw an increase in no-hitters per year, while the recent (and current) Long Ball Era has seen a drop in the mean inter-arrival time of cycles. Triple play mean inter-arrival times are up in recent eras.

The Anderson-Darling Goodness-of-Fit Test was applied to each era for each rare event, to examine whether or not each subset was indicative of exponential behavior (see [Table 6](#)). Note that there are significant departures from “exponentiality” in certain subsets of the data. (We use a significance level of  $\alpha = 0.05$  in what follows.) The data for no-hitters for example, may be exponential in the totality of the data, but is apparently non-exponential in the ‘Lively Ball’ and ‘Free Agent’ eras. Interestingly in the case of triple plays, the process is non-exponential as a total process; however, all but one of the eras fails to reject exponentiality, albeit with different arrival rates. This appears to be evidence of a non-homogeneous Poisson process. Using a Potthoff-Whittinghill test for homogeneity of a Poisson process with parameter lambda unknown (Potthoff and Whittinghill 1966), we reject homogeneity with a very small p-value ( $\ll 0.001$ ). Thus for triple plays, within eras we generally have no reason to reject exponential inter-arrivals, but between eras there are significantly different mean inter-arrival times.

Table 6: Anderson-Darling Goodness-of-Fit Tests

<b>Stat Era</b>	<b>Years</b>	<b>A<sup>2</sup></b>	<b>n</b>	<b>adj A<sup>2</sup></b>	<b>adjusted p-value</b>	<b>Exponential?</b>
<i>all triple plays</i>	1901 - 2004	2.73	511	2.73	< 0.0025	Reject
Dead Ball	1901 - 1919	0.48	107	0.48	> 0.25	Do Not Reject
Lively Ball	1920 - 1941	0.67	136	0.68	> 0.25	Do Not Reject
Integration	1942 - 1960	0.35	81	0.35	> 0.25	Do Not Reject
Expansion	1961 - 1976	1.05	66	1.06	= 0.01	Reject
Free Agent	1977 - 1993	0.51	81	0.51	> 0.25	Do Not Reject
Long Ball	1993 - 2004	0.72	40	0.72	> 0.25	Do Not Reject
<i>all Cycles</i>	1901 - 2004	1.03	225	1.03	0.10 < p < 0.15	Do Not Reject
Dead Ball	1901 - 1919	2.96	22	3.04	< 0.0025	Reject
Lively Ball	1920 - 1941	0.94	60	0.95	0.10 < p < 0.15	Do Not Reject
Integration	1942 - 1960	0.72	29	0.73	> 0.25	Do Not Reject
Expansion	1961 - 1976	0.72	31	0.73	> 0.25	Do Not Reject
Free Agent	1977 - 1993	1.01	46	1.02	0.10 < p < 0.15	Do Not Reject
Long Ball	1993 - 2004	0.90	37	0.91	0.15 < p < 0.20	Do Not Reject
<i>all No-Hitters</i>	1901 - 2004	0.81	206	0.81	0.20 < p < 0.25	Do not Reject
Dead Ball	1901 - 1919	0.96	43	0.97	0.10 < p < 0.15	Do Not Reject
Lively Ball	1920 - 1941	1.43	20	1.47	0.025 < p < 0.05	Reject
Integration	1942 - 1960	0.95	30	0.97	0.10 < p < 0.15	Do Not Reject
Expansion	1961 - 1976	0.63	56	0.64	> 0.25	Do Not Reject
Free Agent	1977 - 1993	1.92	37	1.95	0.01 < p < 0.025	Reject
Long Ball	1993 - 2004	1.08	20	1.11	0.05 < p < 0.10	Do Not Reject

## 5. Conclusion

Historical data on no-hitters, cycles, and triples may be used by students to practice their skill on modeling by the Poisson and/or the exponential distributions. As a part of this modeling process it is important, of course, that students assess the quality of fit. In this paper we demonstrated how to study rare baseball events as Poisson processes, constructing models from the discrete data sets. Using goodness of fit analyses on the inter-arrival times allowed us to assess the exponentiality of the data.

## 6. Getting the Data

The no-hitter data is contained in the Excel file [nohitters.xls](#), the cycles data is contained in the Excel file [cycles.xls](#), and the triple play data is contained in the Excel file [triple plays.xls](#). The file [rarebaseballevents.txt](#) contains a description of the data and, in particular, a listing of the different variables.

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Potthoff, R. F. and Whittinghill, M. (1966), "Testing for Homogeneity: II. The Poisson Distribution", *Biometrika*, 53(1/2), pp. 183-190.

## Internet Sites

Internet site for raw data: [www.retrosheet.org](http://www.retrosheet.org) (access the 'Outstanding Feats' link) accessed 1 Oct 2004.

Internet site for triple play data: [tripleplays.sabr.org/tp\\_sum.htm](http://tripleplays.sabr.org/tp_sum.htm) accessed 1 Jul 2006.

Internet site for hitting for the cycle facts: [www.Baseball-Almanac.com/feats/feats16d.shtml](http://www.Baseball-Almanac.com/feats/feats16d.shtml) accessed 1 Oct 2004.

Internet site for no-hit game definition: [mlb.mlb.com/NASApp/mlb/mlb/official\\_info/official\\_rules/foreword.jsp](http://mlb.mlb.com/NASApp/mlb/mlb/official_info/official_rules/foreword.jsp) accessed 11 Feb 06.

Internet site for baseball eras: [www.netshrine.com/era.html](http://www.netshrine.com/era.html) accessed 10 Feb 2006.

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